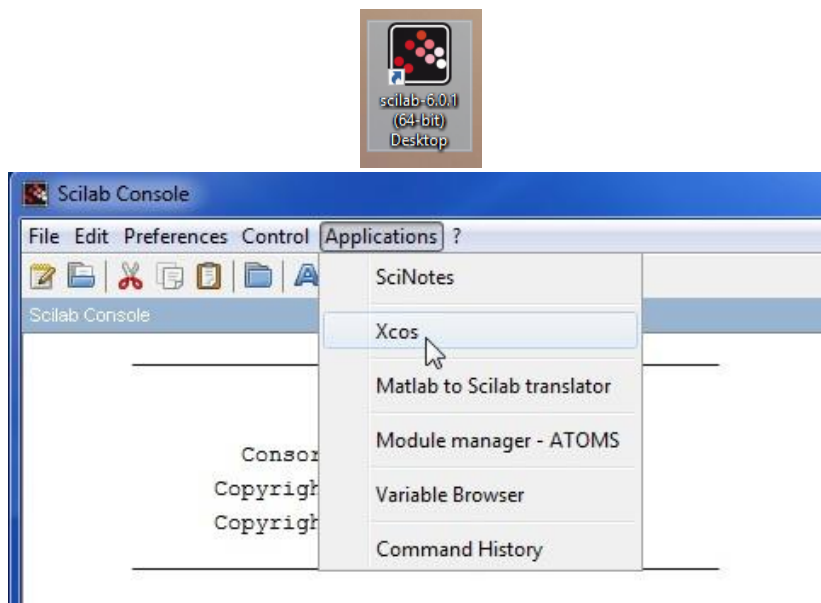
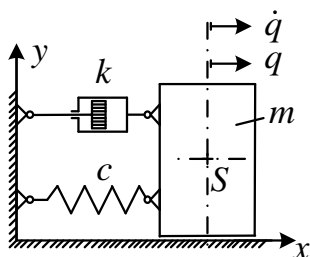


Dynamics of Machines Week 5 –1st and 2nd Exercises



5/1 Exercise - Free Vibration of a Single Degree of Freedom System (Xcos)



$$m\ddot{q} + k\dot{q} + \frac{1}{c}q = 0$$

$$\ddot{q} = \frac{1}{m} \left(-k\dot{q} - \frac{1}{c}q \right) = -\frac{k}{m}\dot{q} - \frac{1}{cm}q = -\frac{0.9}{5}\dot{q} - \frac{1}{0.5 \cdot 5}q = 0$$

$$\ddot{q} = -\frac{0.9}{5}\dot{q} - \frac{2}{5}q \quad (\text{acceleration})$$

$$k = 0.9 \frac{Ns}{m} \quad - \text{damping coefficient}$$

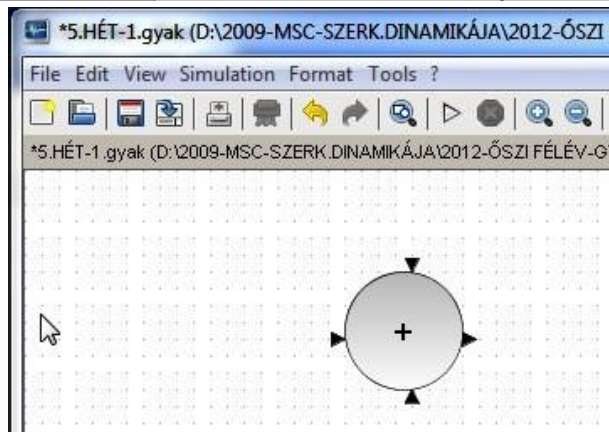
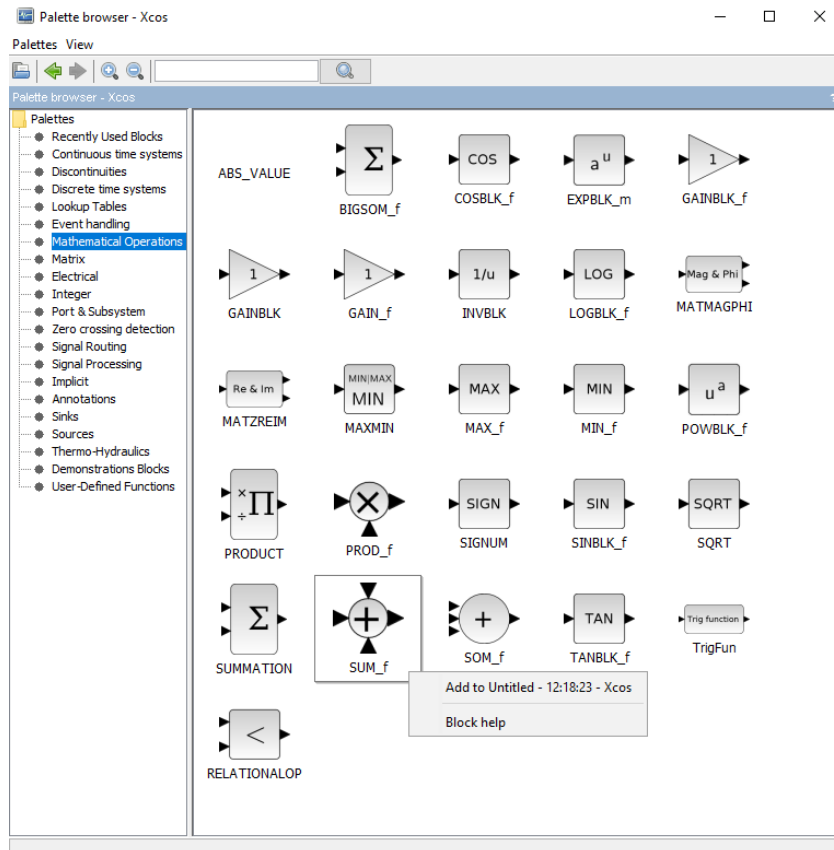
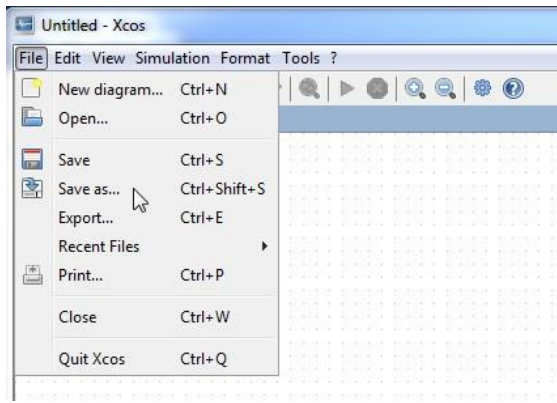
$$c = 0.5 \frac{m}{N} \quad - \text{spring constant}$$

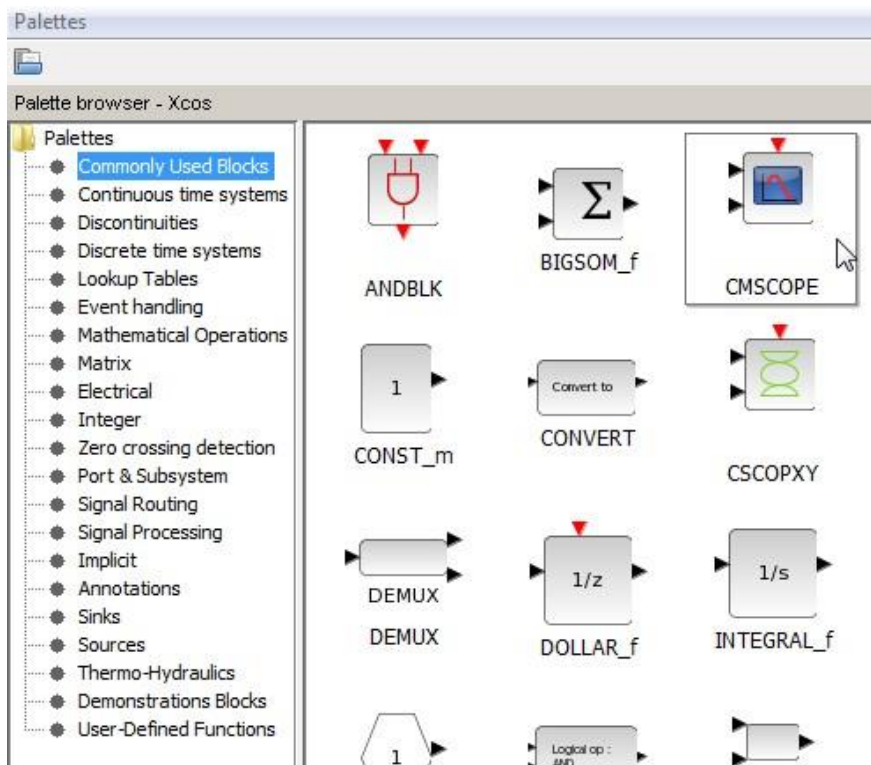
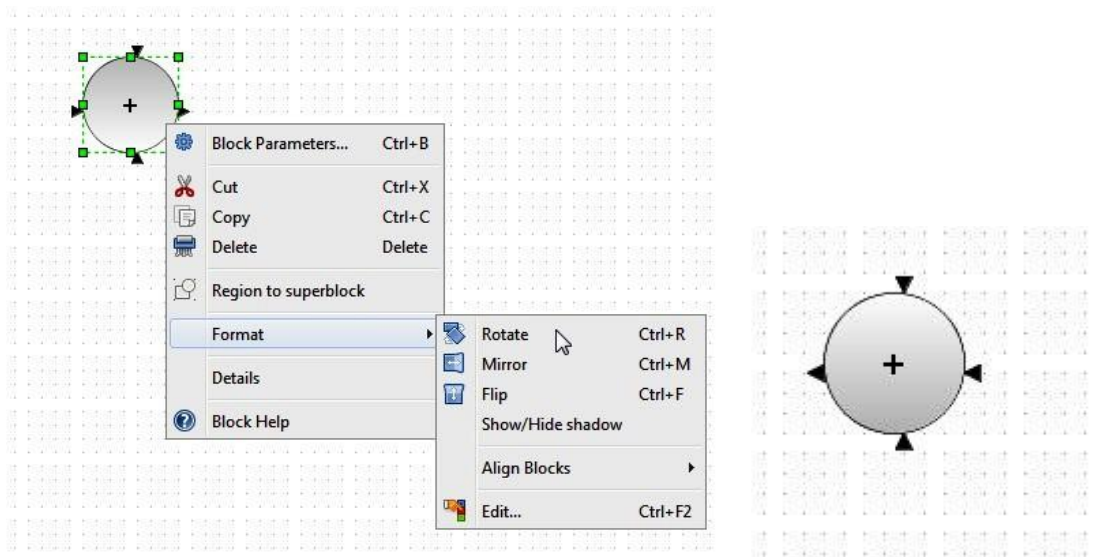
$$m = 5 \text{ kg} \quad - \text{mass}$$

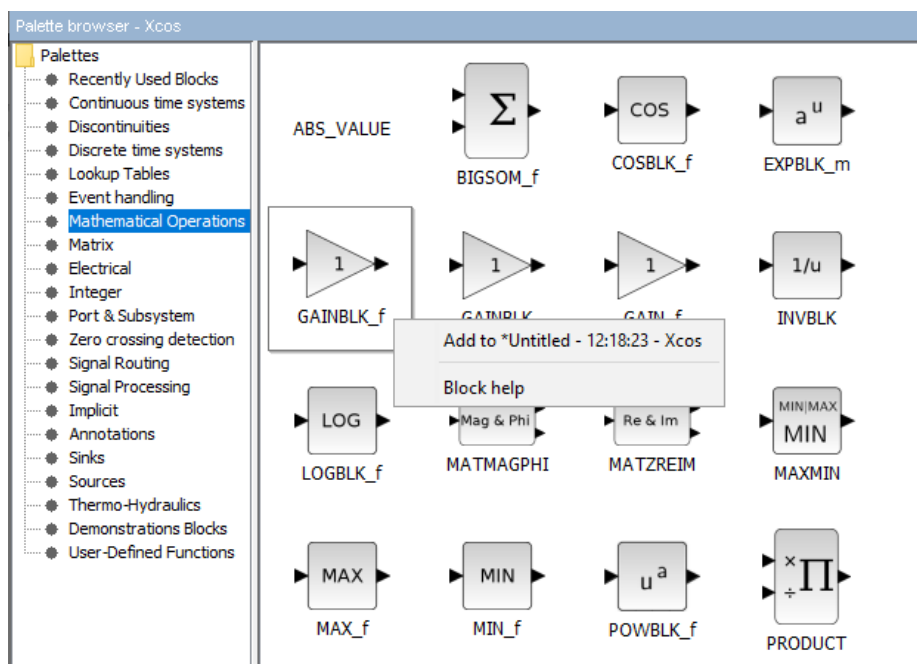
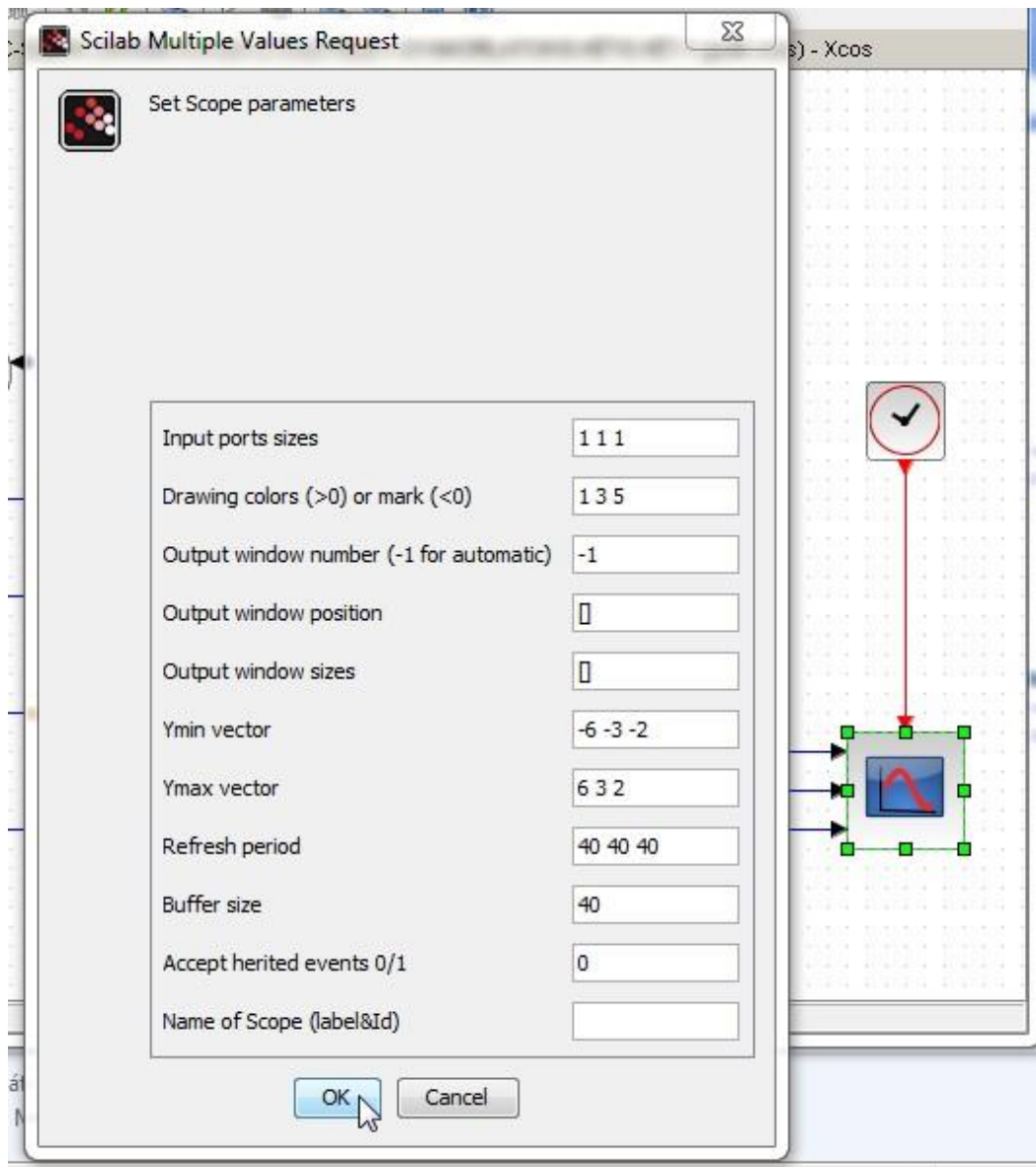
Initial Conditions:

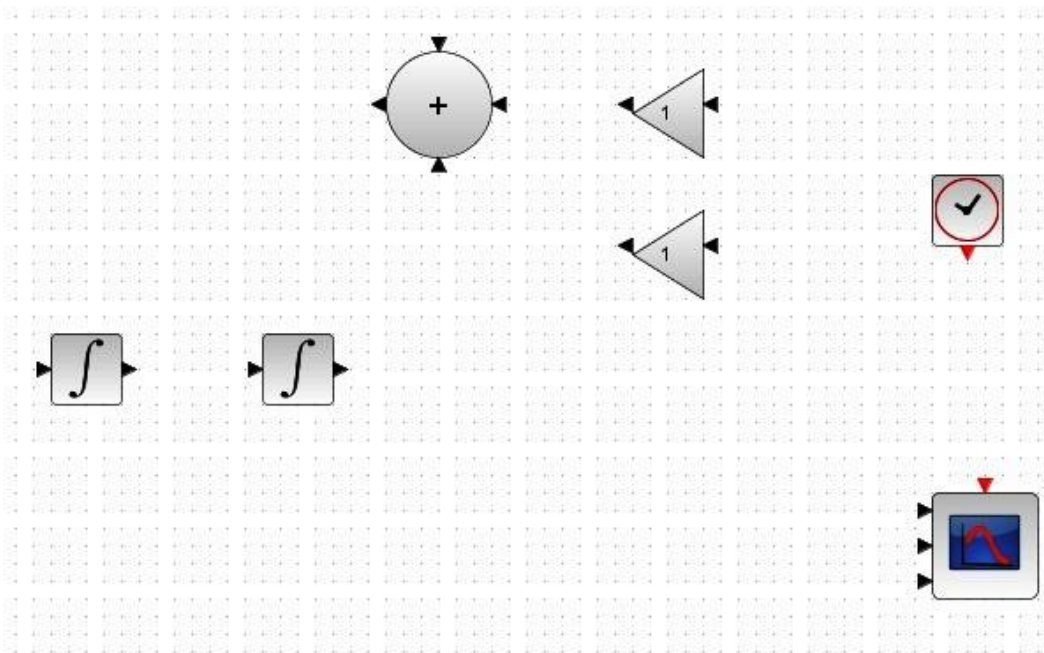
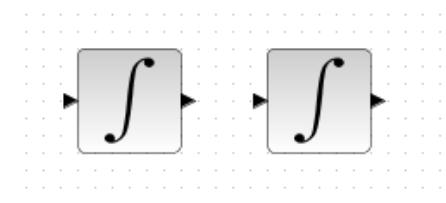
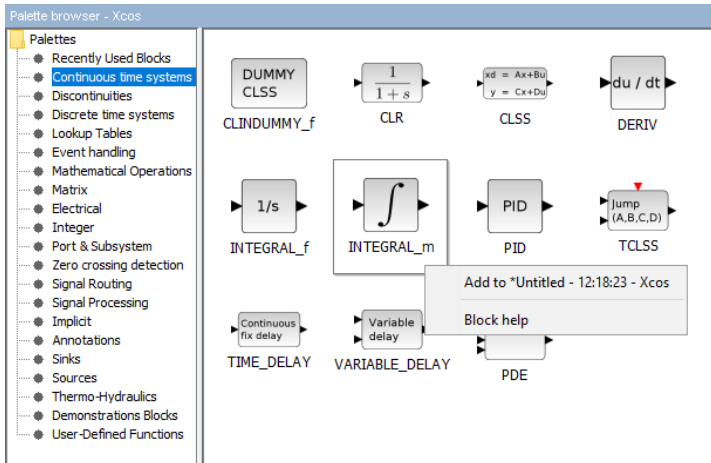
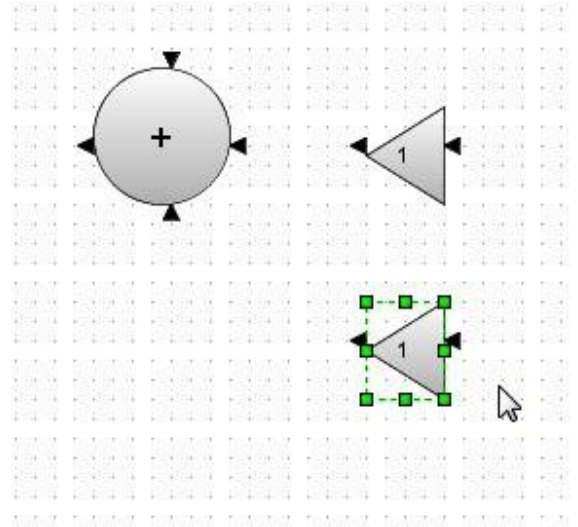
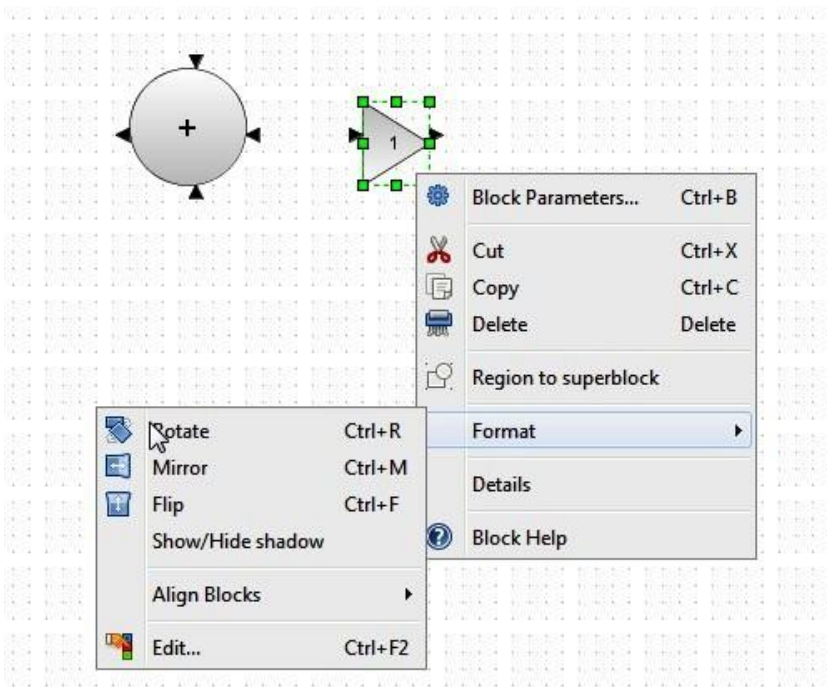
$$q_0 = 1 \text{ m} \quad - \text{initial displacement}$$

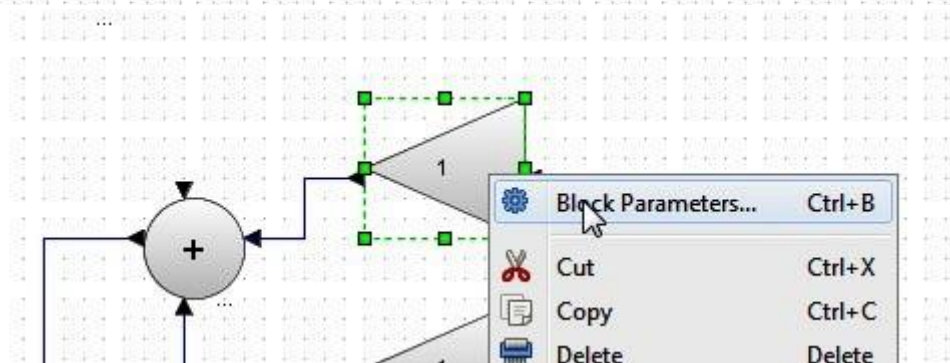
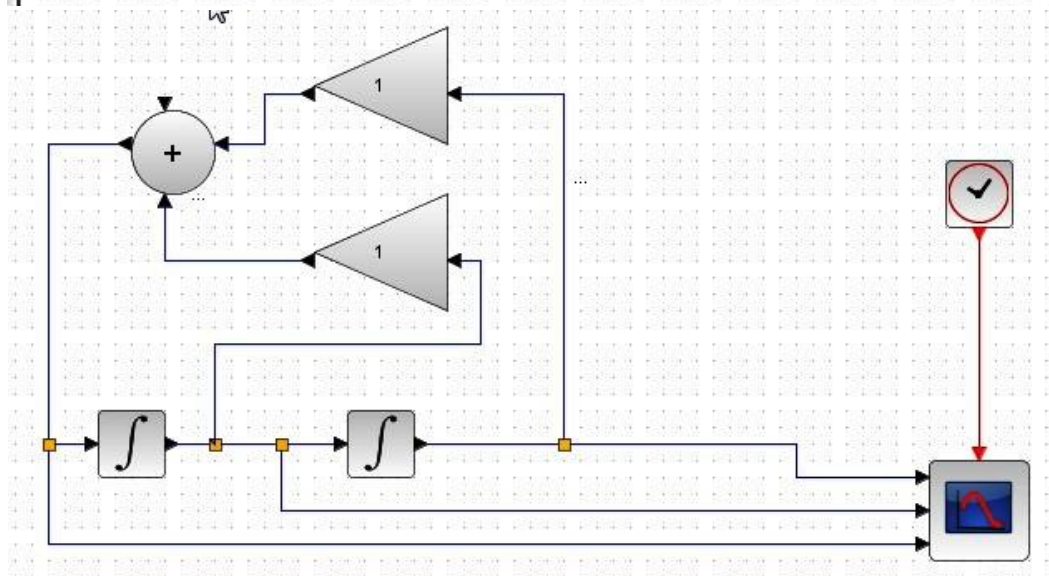
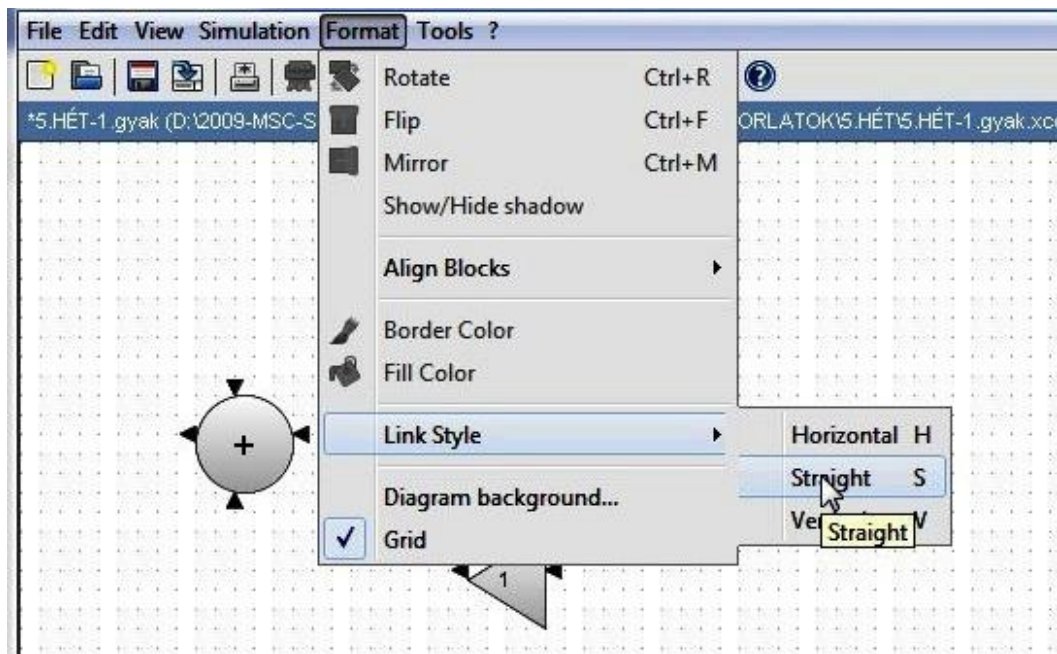
$$\dot{q}_0 = 3 \text{ m/s} \quad - \text{initial velocity}$$

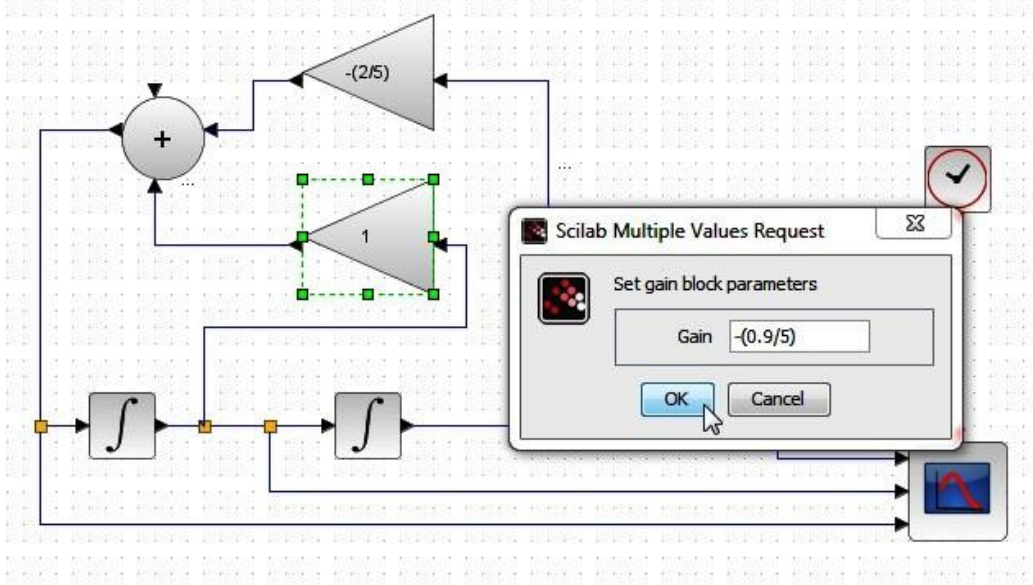
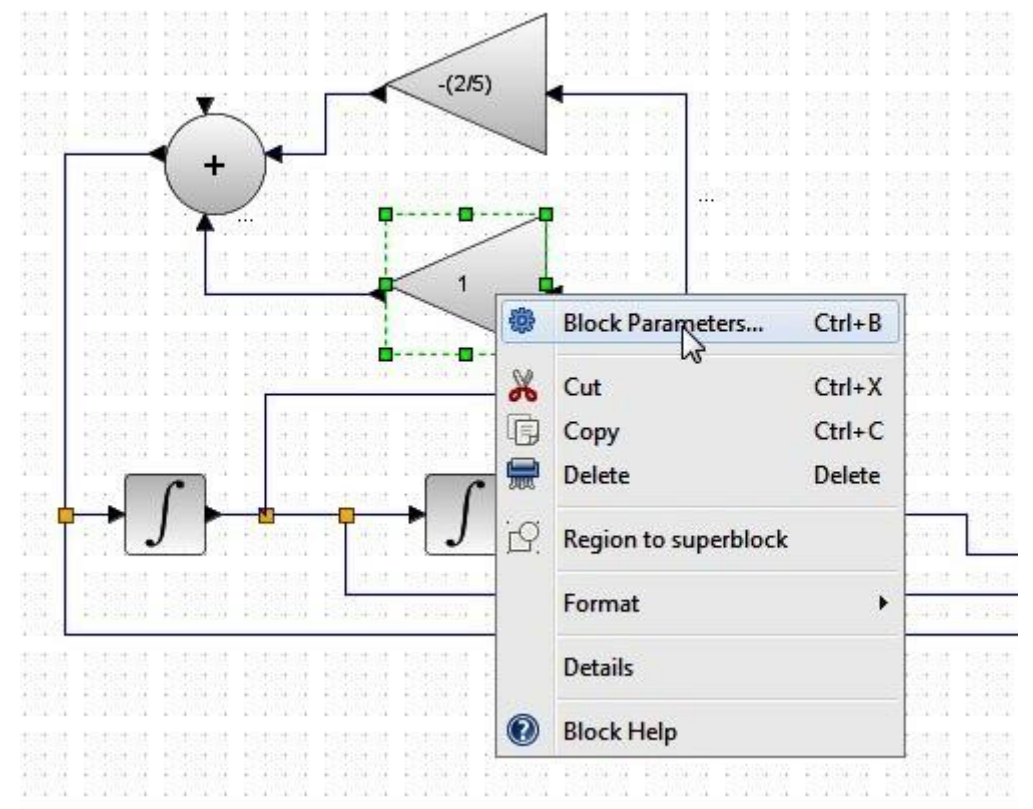
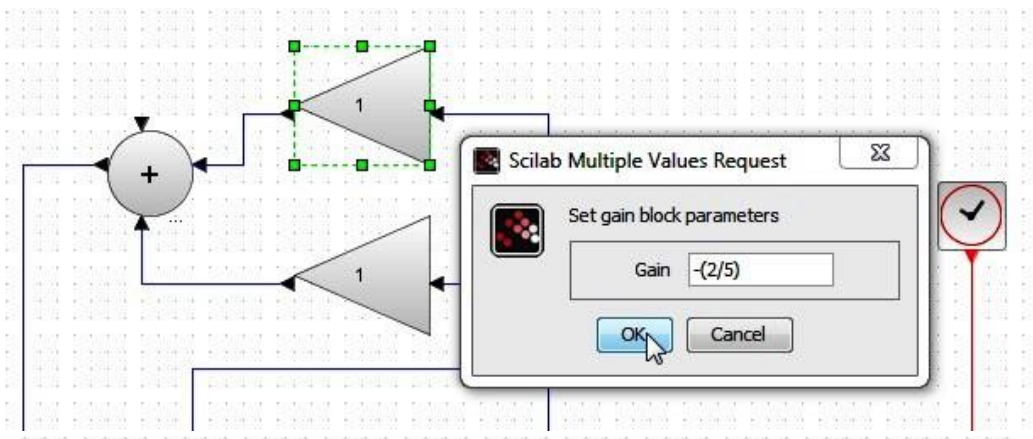


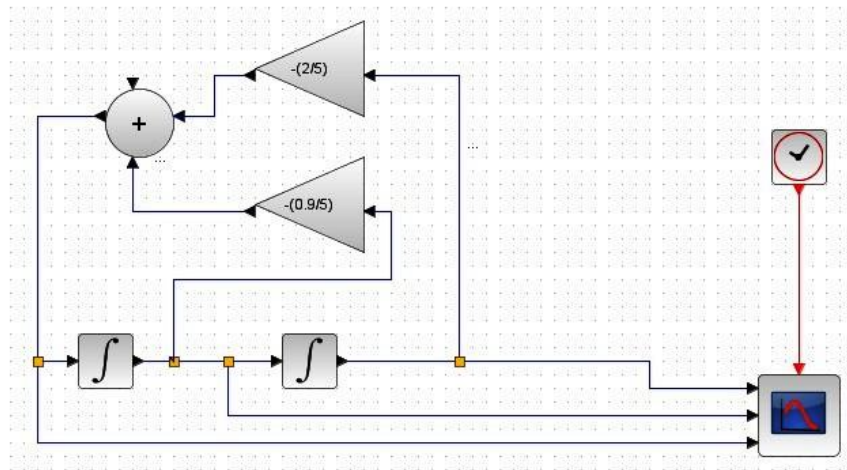
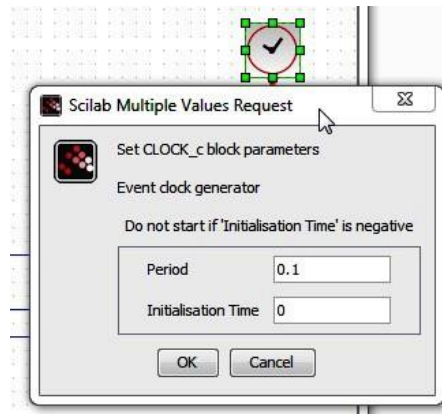




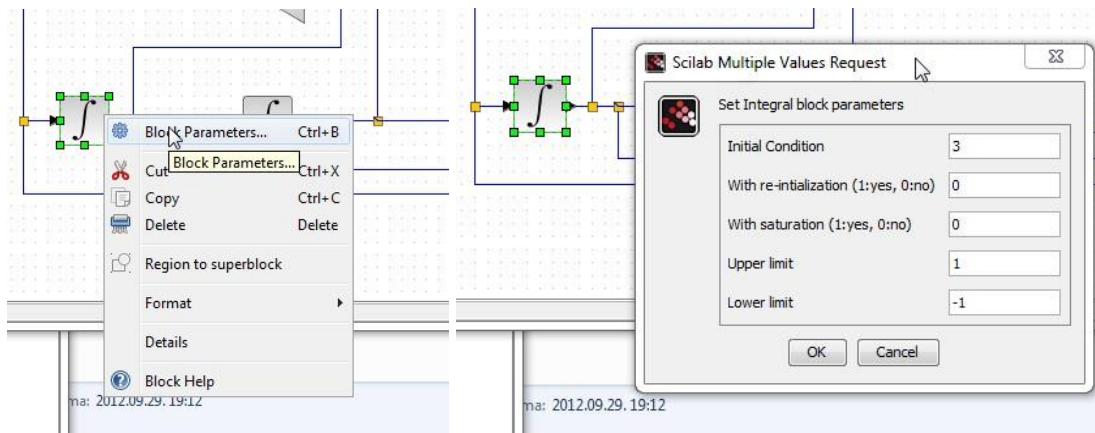




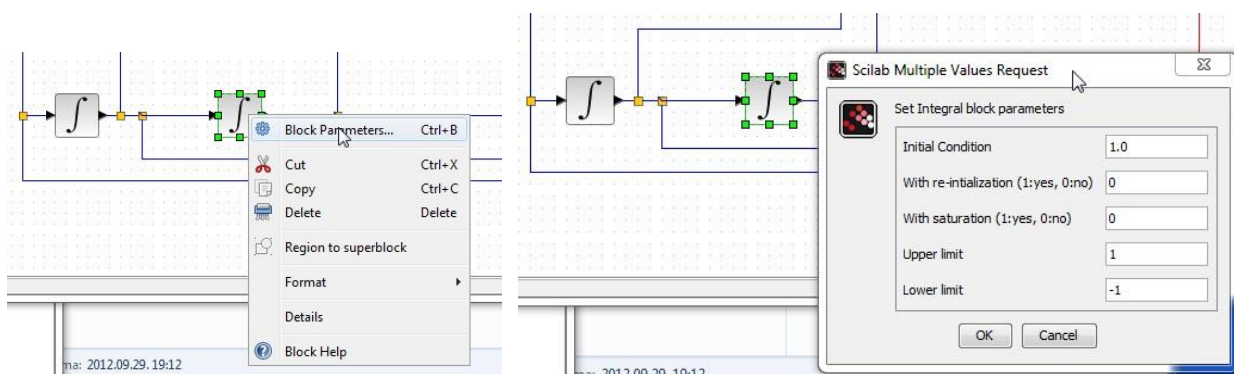




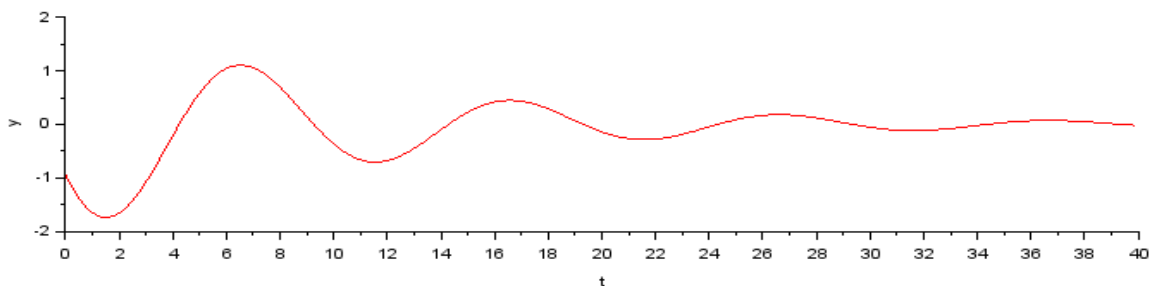
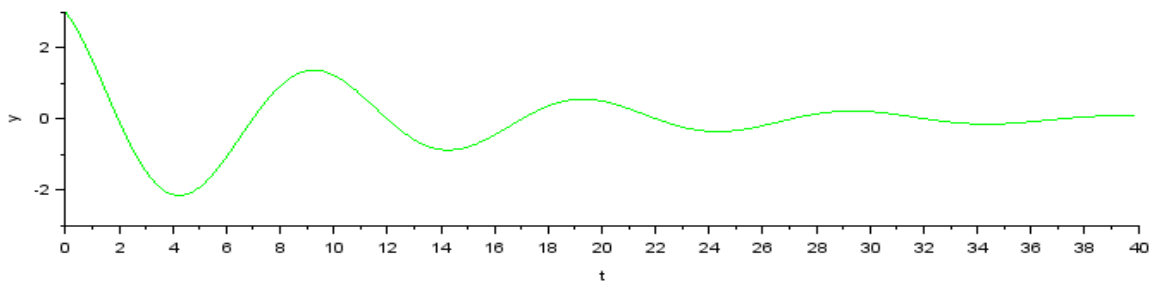
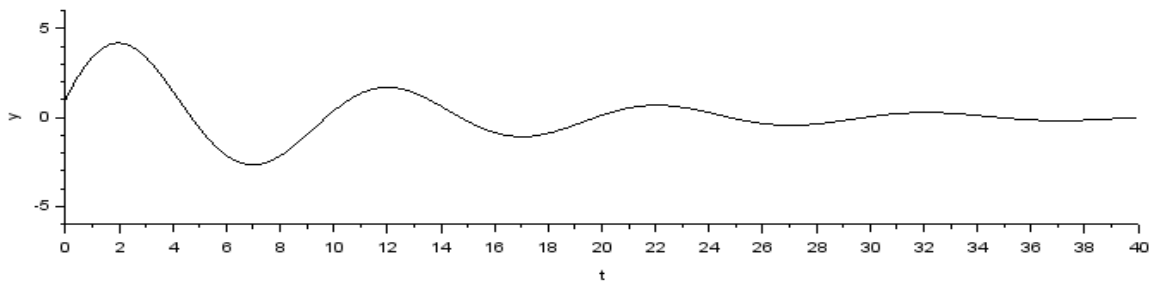
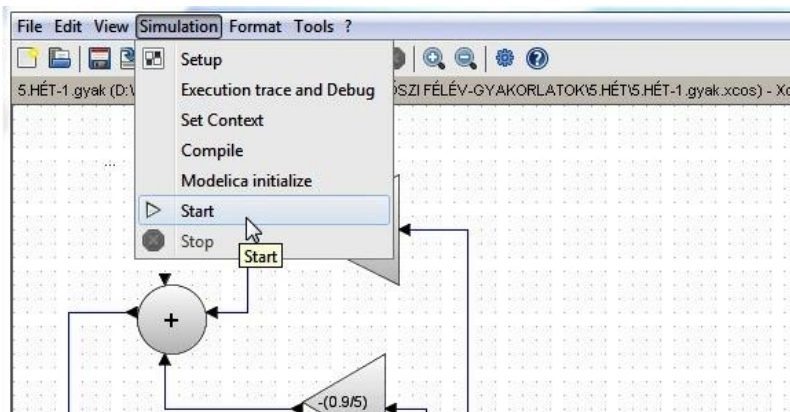
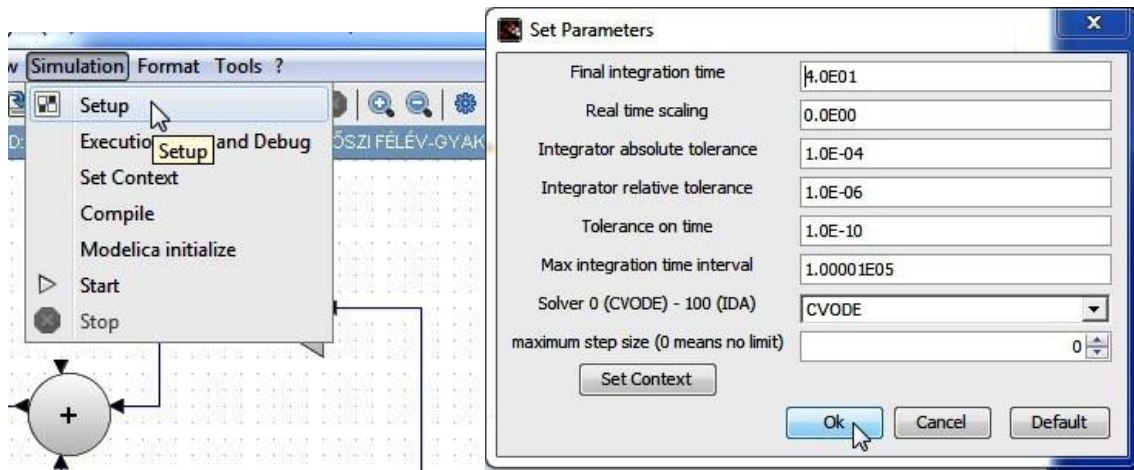
Initial velocity: 3 (m/s)



Initial displacement: 1 (m)

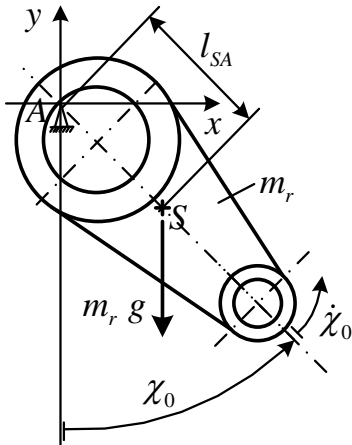


Final integration time: 40 (s)



5/2 Exercise – Physical Pendulum (Xcos)

$$J_{AZ} \ddot{\chi} = -l_{SA} m_r g \sin \chi$$



$$\ddot{\chi} = -\frac{l_{SA} m_r g}{J_{AZ}} \sin \chi \quad (\text{rad} / \text{s}^2) \quad \text{angular acceleration}$$

$$l_{SA} = 0,15 \text{ m} \quad J_{AZ} = 0,05 \text{ kgm}^2$$

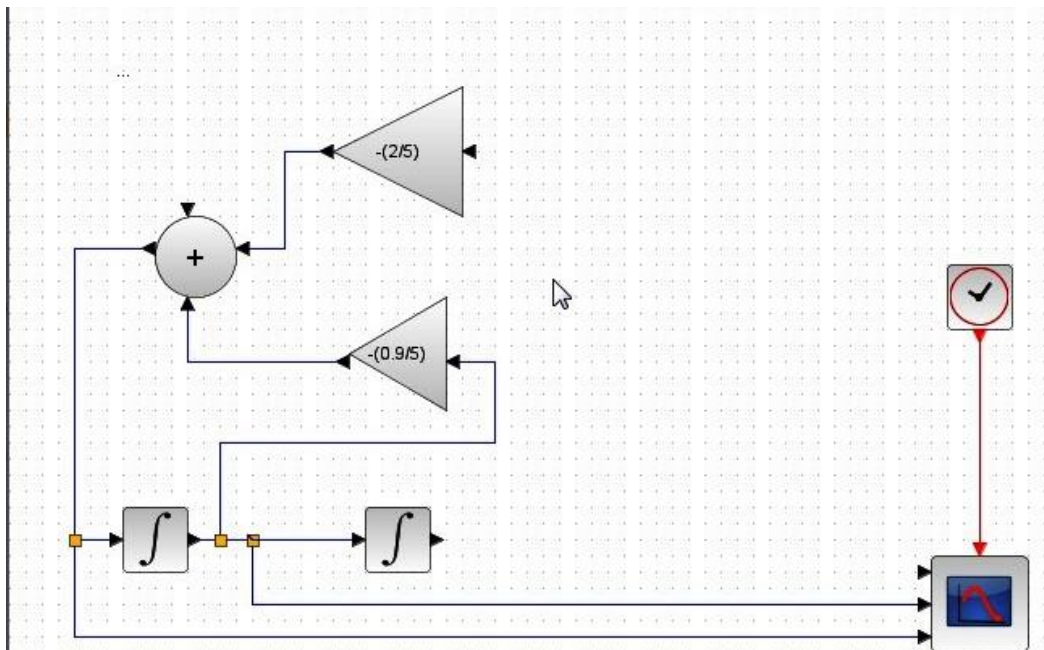
$$m_r = 0,45 \text{ kg} \quad g = 10 \frac{\text{m}}{\text{s}^2}$$

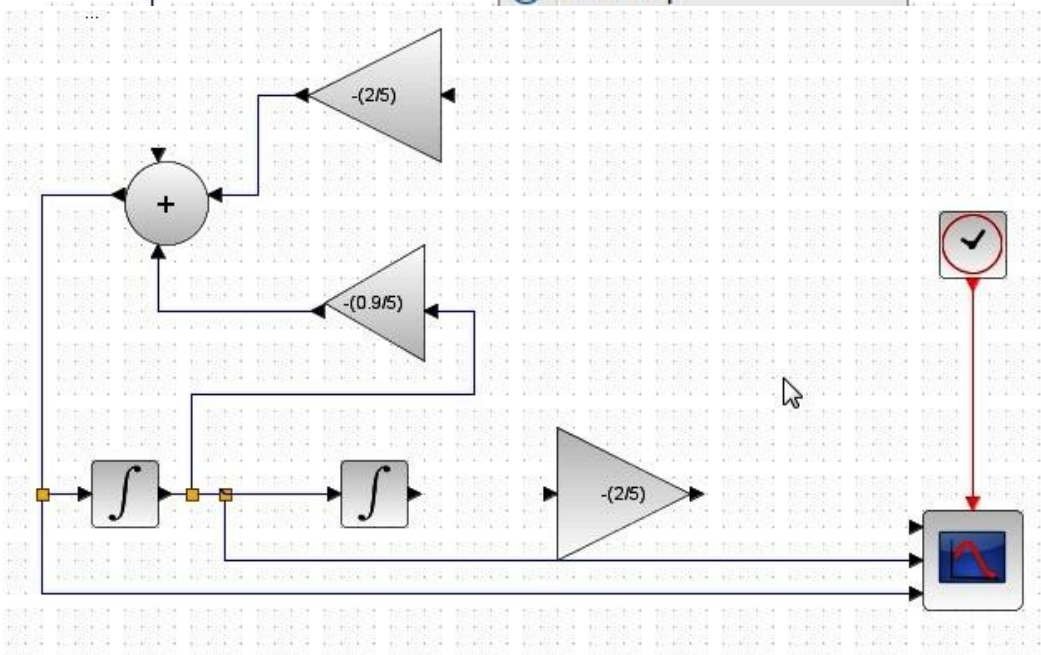
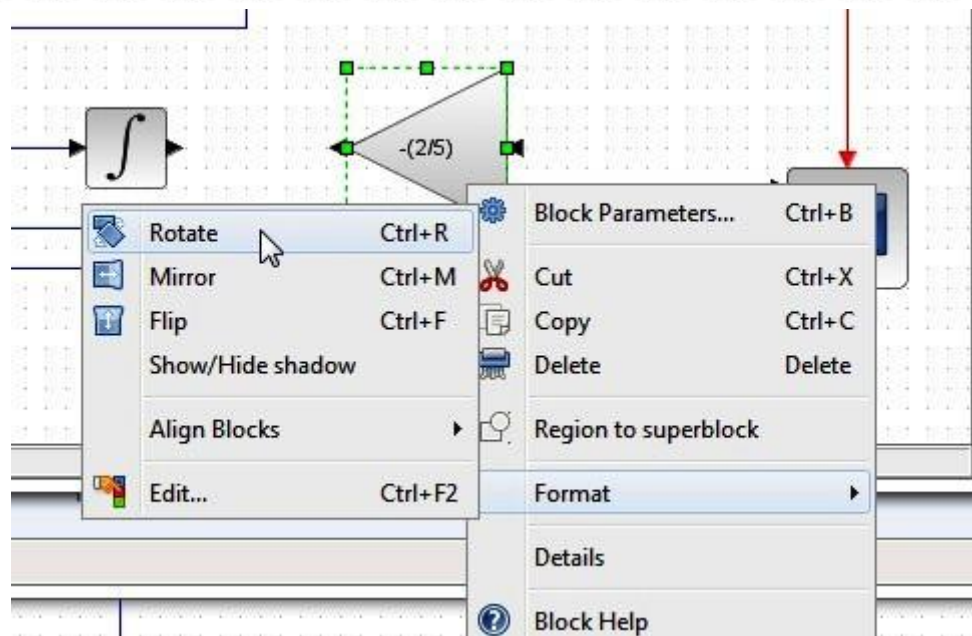
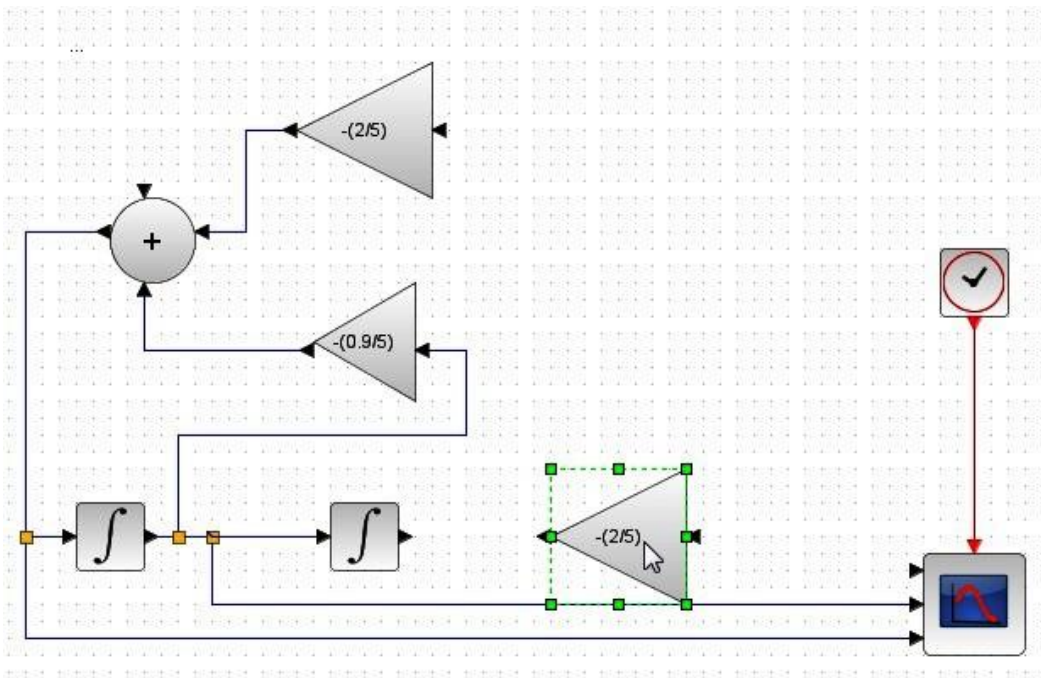
Initial Conditions:

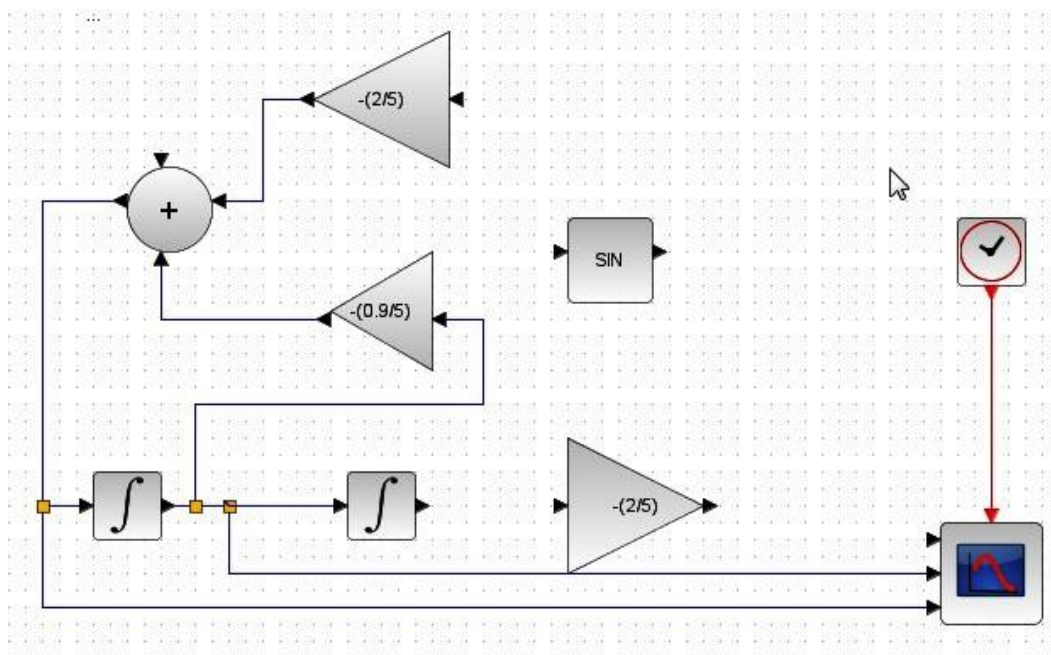
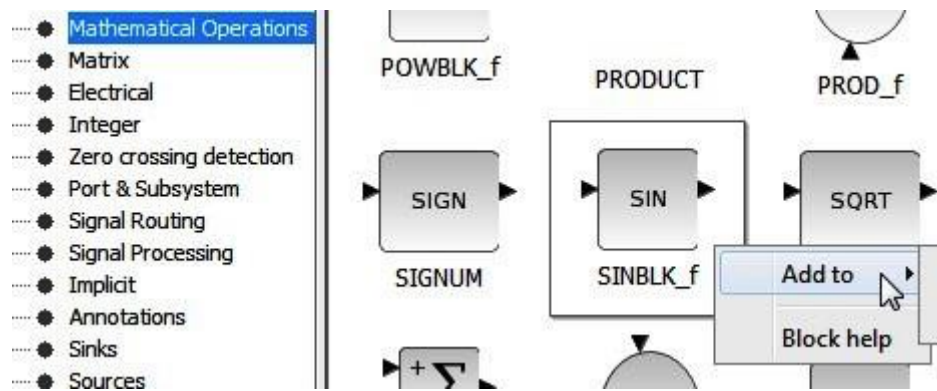
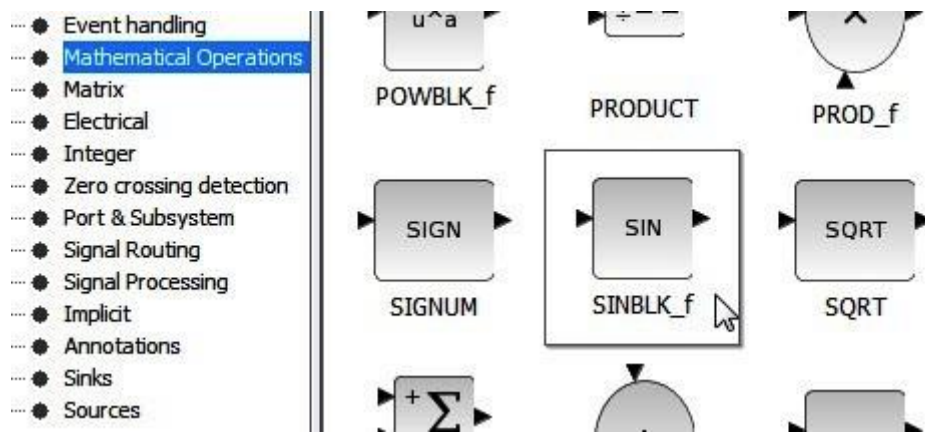
$$\chi_0 = 120^\circ \quad - \text{ initial angle}$$

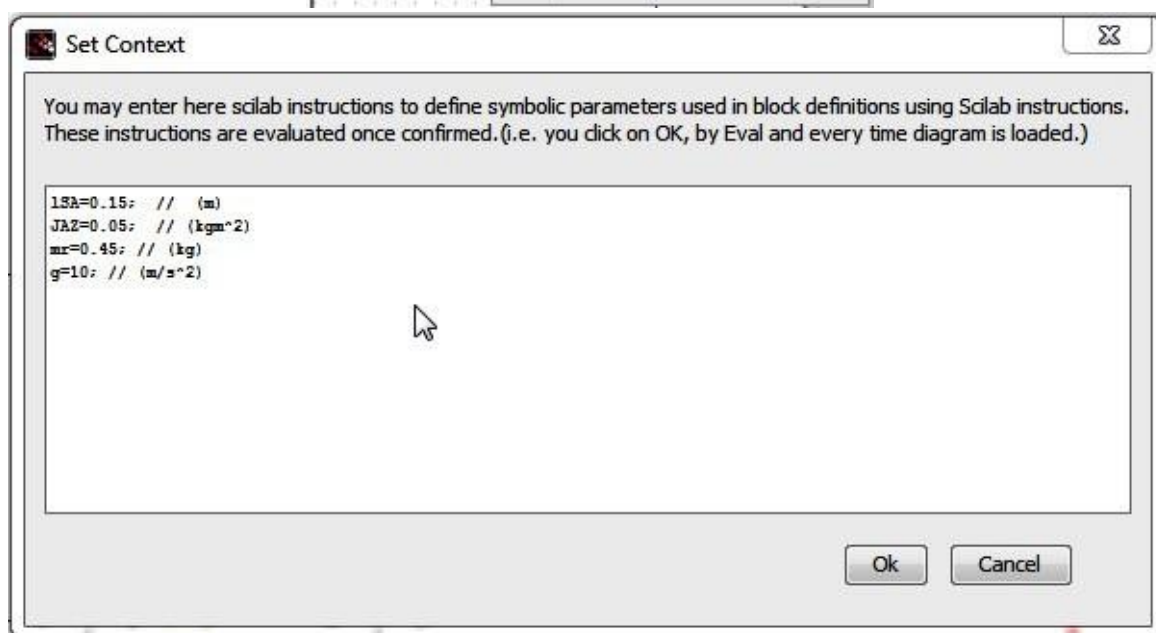
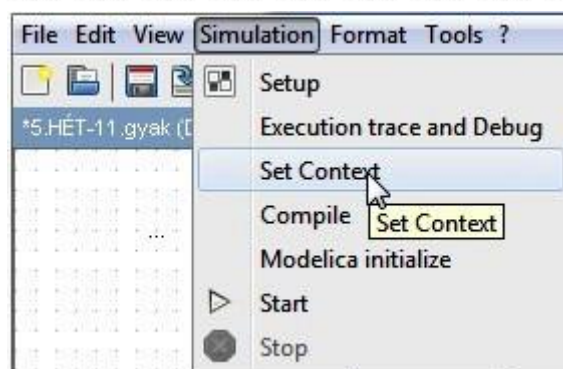
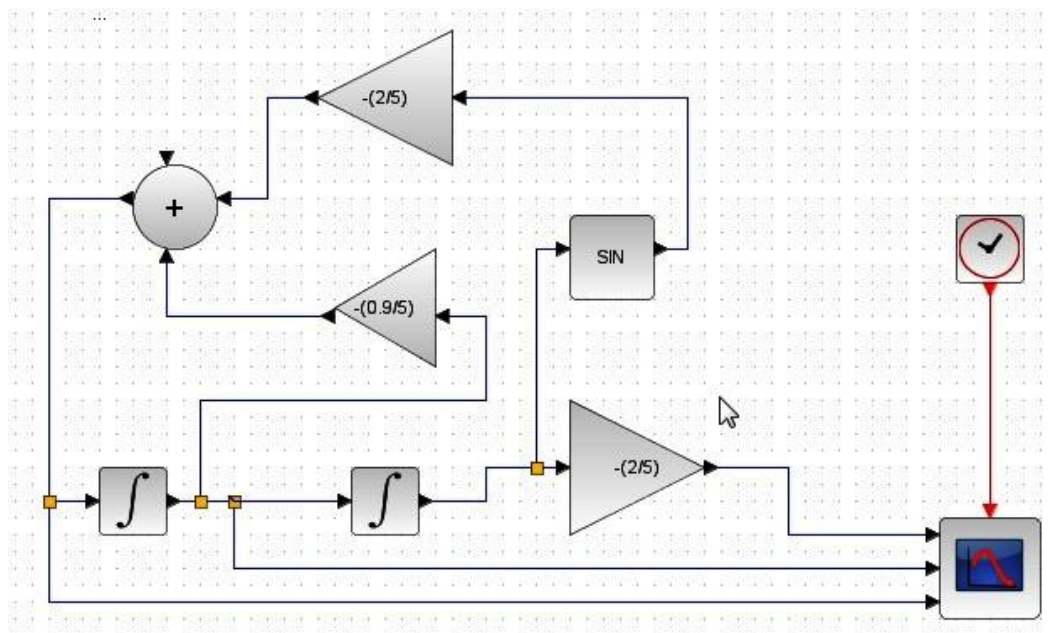
$$\dot{\chi}_0 = 0,5 \frac{\text{rad}}{\text{s}} \quad - \text{ initial angular velocity}$$

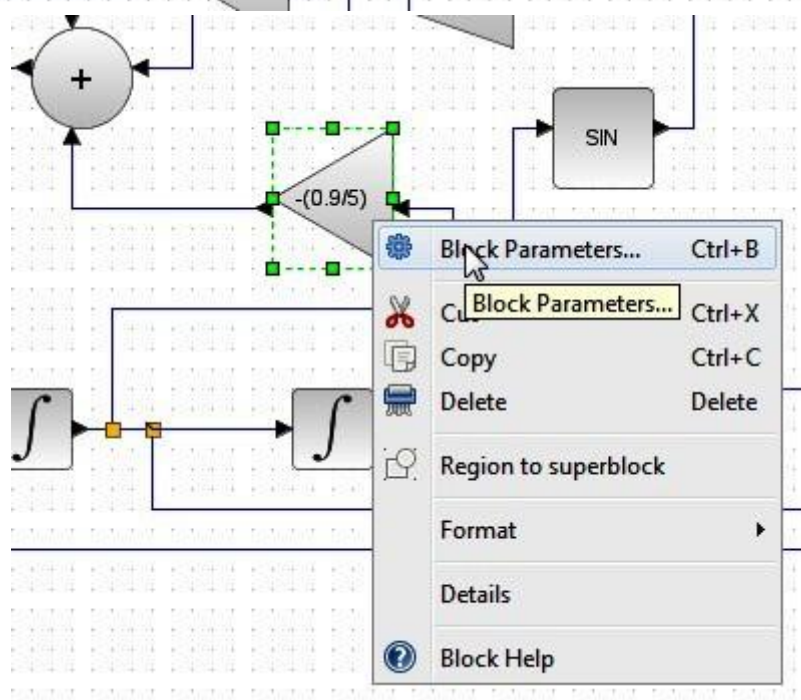
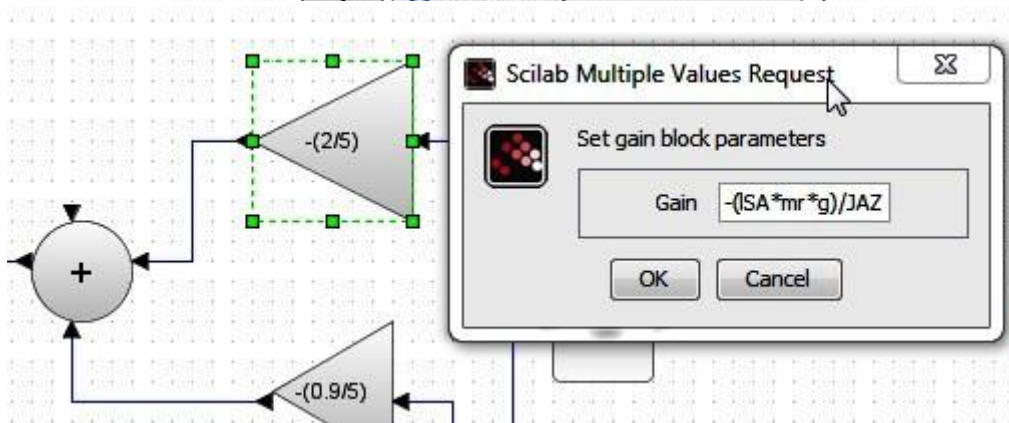
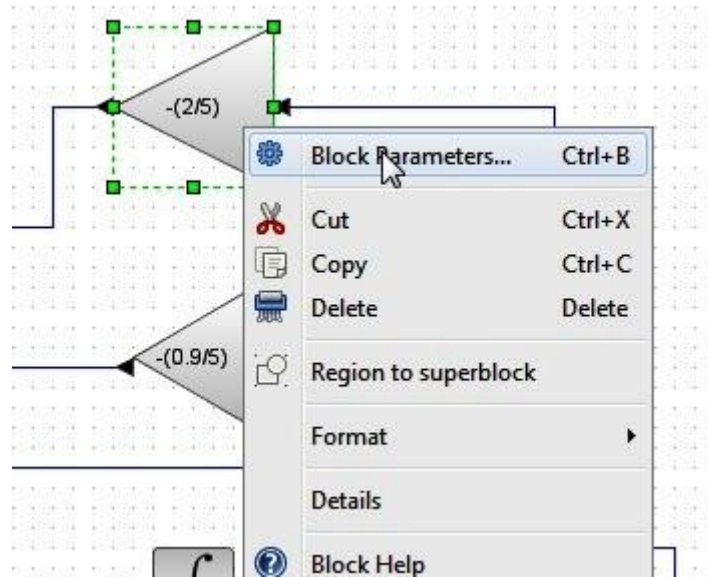
Let's modify the previous xcos model as it is in the pictures below and save the new model.

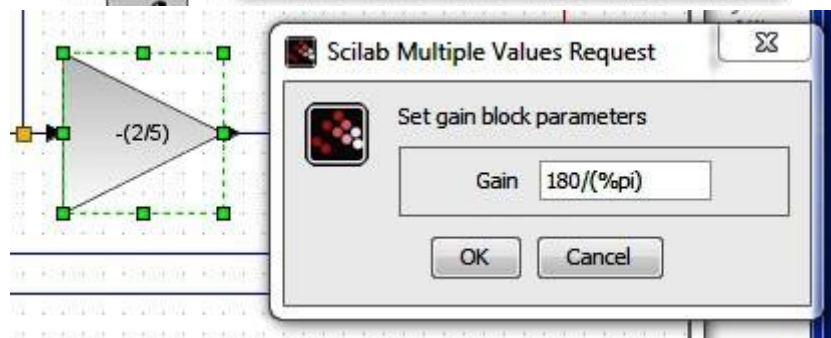
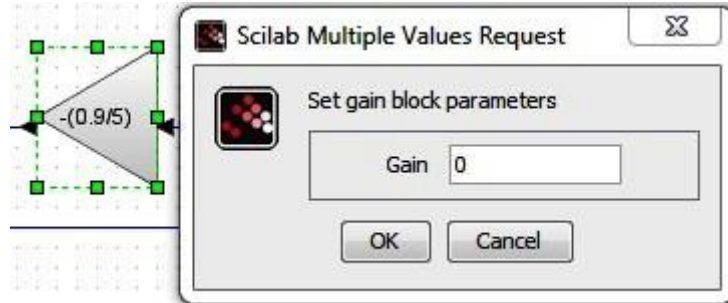
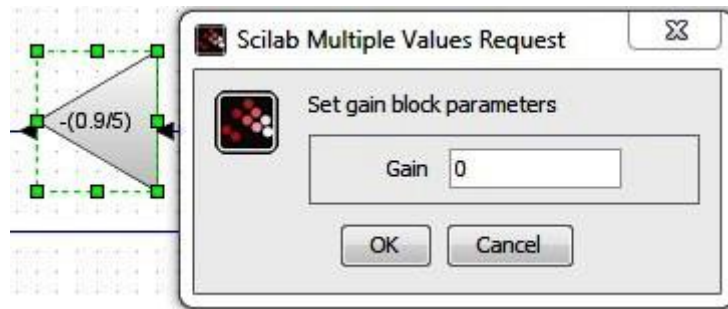




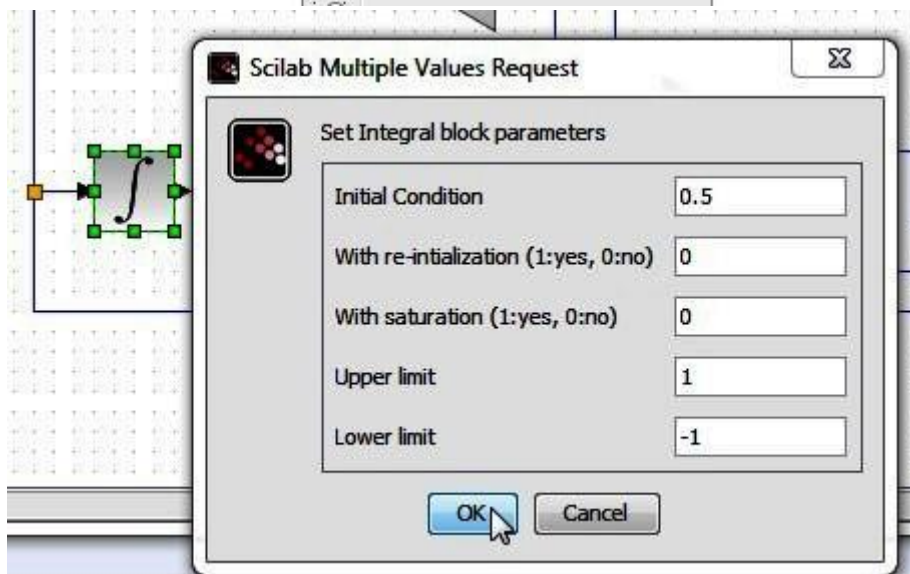
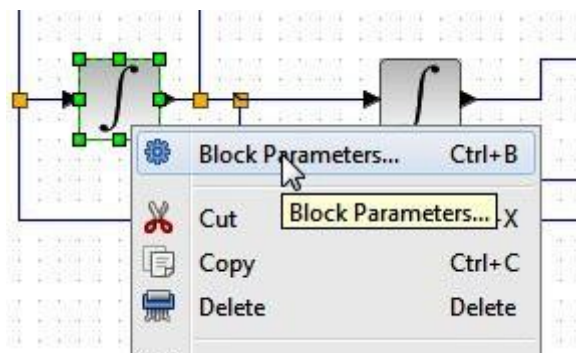




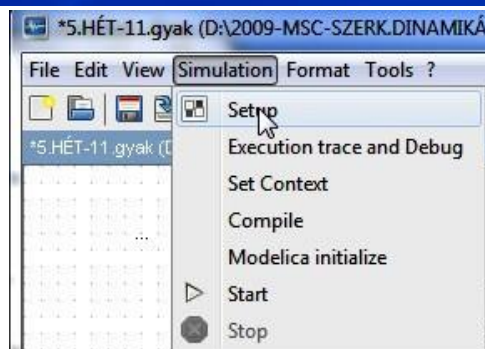
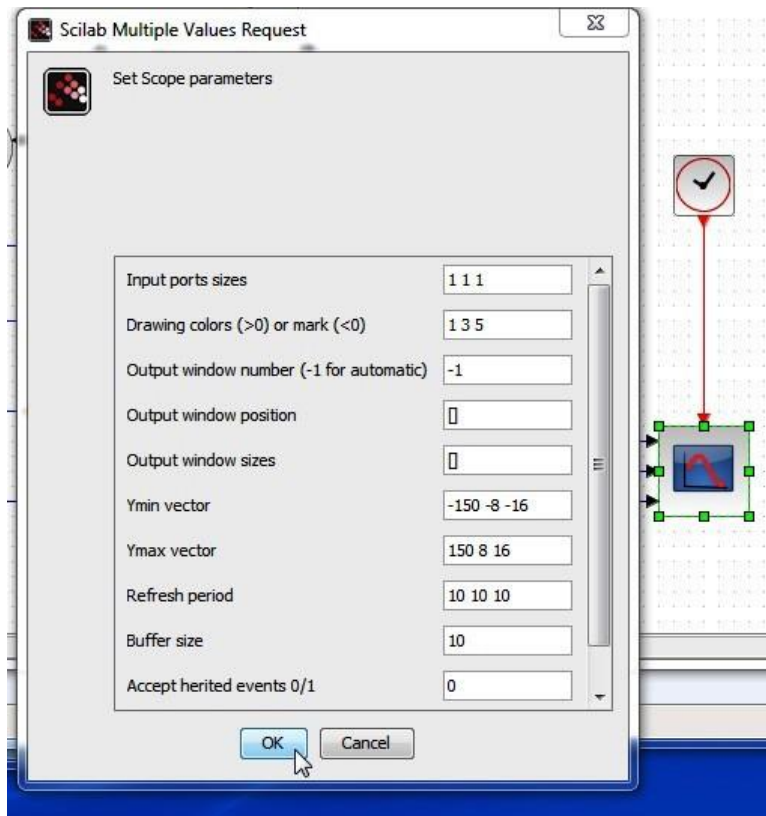
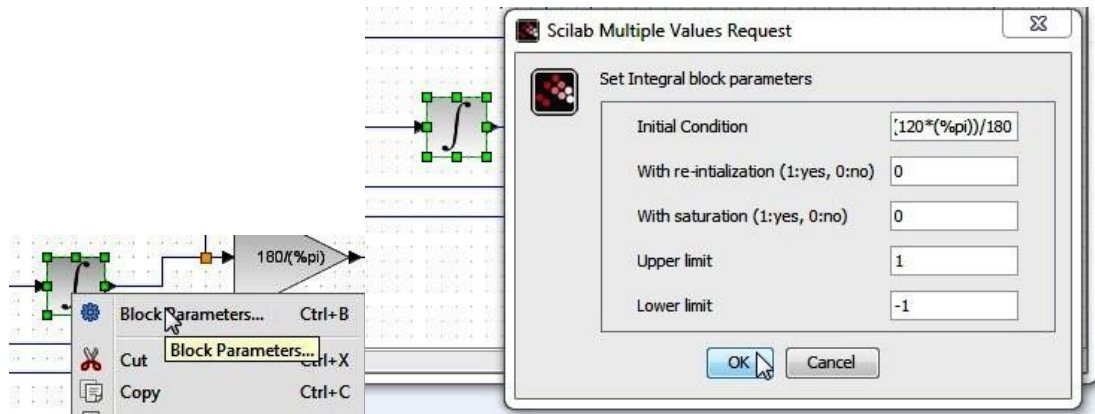




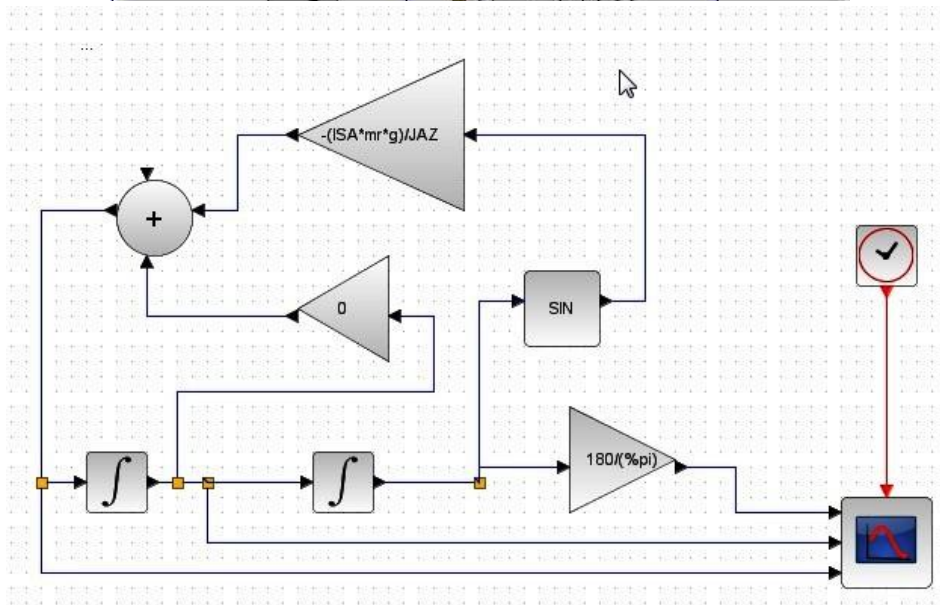
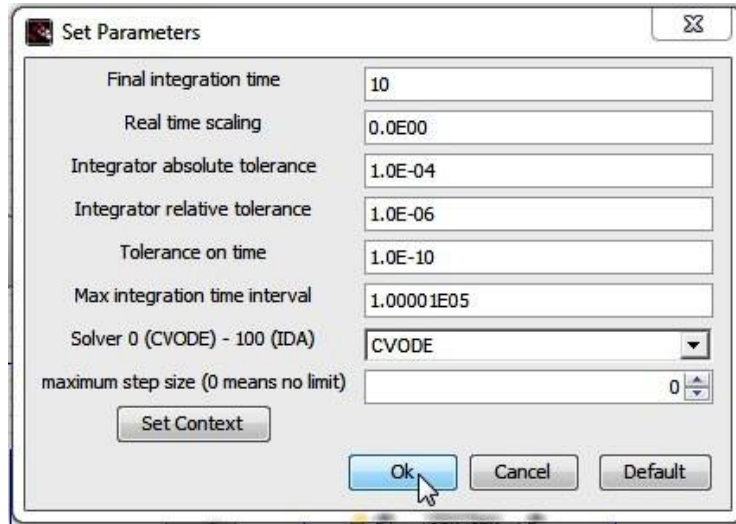
Initial angular velocity: 0.5 (rad/s)



Initial angle: 120 degrees = $120 \cdot \pi / 180$ rad



Final integration time: 10 (s)



Run the xcos model:

